

2

$$\begin{aligned}
 \text{a) } c &= 76/12.5 = 6.08 \\
 k &= Gd/8\pi^2 c^3 = 79G3 \times 12.5 / 8 \times 5 \times 6.08^3 \\
 &\quad \text{mm/mm} - \text{from (2)} \\
 \text{b) } l_s &= \frac{110}{k} \text{ N/mm} \\
 l_s &= \frac{n_t d}{(n_t + 2)d} = (n_t + 2)12.5 = 87.5 \text{ mm} \\
 &\quad - \text{from Table 1.} \\
 \therefore l_s &= (6 - l_s) = 140 - 87.5 = 52.5 \text{ mm} \\
 \therefore F_s &= k l_s = 110 \times 52.5 = 5775 \text{ N} \\
 T_s &= K_s \cdot 8 F_s / \pi d^2 \quad \text{from (1)} \\
 T_s &= 8 \times 5775 (6.08 + \frac{1}{2}) / \pi \times 12.5^2 = 610 \text{ Nm} \\
 \text{c) } F &= 3000 \text{ N} \quad F = 2000 \text{ N} \\
 \therefore F_m &= 2500 \text{ N} \quad \& F_d = 500 \text{ N.} \\
 \text{From (5b),} \\
 F_e &= \frac{2F_m CK_r}{S_{ut}/S_{ut}} + \frac{2F_d CK_h}{S_{ut}/S_{ut}} \\
 &= \frac{2 \times 2500 (6.08 + \frac{1}{2})}{0.63} + \frac{2 \times 500 \times 6.08}{0.13} \frac{6.08 + 0.6}{6.08 - 0.6} \\
 &\quad - \text{using Table 1} \\
 &= 110 \text{ kN.}
 \end{aligned}$$

Whereas $F_{ut} = 142 \text{ kN}$ from table
 $\therefore n = 142/110 = 1.29$. say $\frac{1.2}{2}$

5

$$\begin{aligned}
 \text{Since zero-to-max endurance limit is known,} \\
 \text{use (4a). } F = 250 \quad F = 500 \quad \therefore \bar{F} = 375 \quad \bar{F} = 125 \text{ N.} \\
 T_m &= CK_s \cdot 8 \bar{F} / \pi d^2 \quad \text{set } A = \frac{\pi}{4} d^2 \text{ as the unknown (mm}^2\text{)} \\
 &= CK_s 2 \bar{F} / A = (6 + 0.5) 2 \times 375 / A = 5625 / A \text{ Nm.} \\
 T_d &= CK_h 2 \bar{F} / A = \frac{7.6}{6.75} \times 2 \times 125 / A = 2101 / A \text{ Nm.} \\
 (\text{4a) } 5625/A \times 1000 + (2101/A)(\frac{2}{550} - \frac{1}{1000}) &= 4n \quad * \\
 \text{Selecting } n = 1.2 \text{ say } \Rightarrow A = 13.4 \text{ mm}^2 \quad d = 4.1 \text{ mm} \\
 \text{Use } d = 4 \text{ mm with } n = 1.13 \text{ from *} \\
 \text{Check static yield at } \bar{F} = 500 \text{ N.} \\
 \tau_{dy} &= CK_s F_{dy} 8 / \pi d^2 = 7.5 \times 500 \times 8 / \pi \times 4^2 = 597 \text{ MPa} \\
 &\quad \text{which is } < S_y = 680 \text{ MPa - so OK.} \\
 \text{No information given on stiffness or deflections} \\
 \text{so can't examine buckling etc.}
 \end{aligned}$$