

Safety factor of 1.5 at highest operating point (7 kN , 50 mm).
So yield at 10.5 kN . Take solidification at ~~that~~ say 1 kN , so that yield impossible.
Essentially static - use K_s from(1) $\frac{F}{d^2} = K_s$, $8FC/500d^2 \leq S_y/s/u$

$$\therefore K_s \cdot 8 \times 7 \times 3 \text{ C} / 500d^2 \leq 600 / 1.5$$

$$\text{i.e. } d^2 \geq 38.75 \text{ C} / K_s = 38.75 (\text{C} + \frac{1}{2})$$

For $\alpha = 1$ practical first choice take $5 \leq C \leq 10$
 $14.6 \leq d \leq 20.2 \text{ mm}$.

so consider two trial solutions of d in this range:

$$\begin{array}{lll} \text{d :} & (6 & 20 \text{ mm}) \\ \therefore \text{Cmax from static } 6.1 \frac{20^2}{300\pi} - \frac{1}{2} = 9.8 & \\ \text{from(2)} \quad u_2 \geq 6d / 8kC^3 \quad (\text{since } \delta_{\text{max}} \text{ given}) & \\ = 75 \times 10^3 d / 8 \times (2000/50) C^3 & \\ \therefore u_2 \text{ (mm).} & 5.0 \quad 1.5 \text{ factors} \\ D_o = (e+1)d. & (mm) \quad 114 < 150 \quad \text{OK.} \end{array}$$

Completing the specification $d = 16 \text{ mm}$ $C = 6.1$
 $D = e d = 6.1 \times 16 = 98 \text{ mm}$.

$$2b = D + d = 98 + 16 = 114 < 150 \text{ mm, so OK.}$$

Assuming serrated & ground ends.

$$u_p = u_2 + 2 = 5 + 2 = 7$$

From the characteristic, when solid

$$S_s = 9 \times (50/7) = 64 \text{ mm.}$$

$$\therefore L_s = u_p d. \quad (\text{table 1}) = 7 \times 16 = 112 \text{ mm.}$$

$$\therefore L_o = L_s + S_s = 112 + 64 = 176 \text{ mm.}$$

$$L = u_p p + 2d = 5p + 2 \times 16 \quad (\text{table 1})$$

$$\Rightarrow p = 28.8 \text{ mm}$$

$$\text{i.e. } \alpha = \frac{\text{act. } p / \pi D}{\text{act. } D} = \frac{28.8}{98\pi} = 5.3^\circ - \text{close ended OK}$$

The solution is fairly satisfactory though active stress is rather low.
might try smaller index, eg taking $C = 10/16 = 5.62 \Rightarrow u_2 = 6.34$ (from *)

— and so on.

There appear to be no criteria which could further tune the design.

$$\text{So } d = 16 \text{ mm} \quad D = 98 \text{ mm} \quad u_p = 7$$

$$L_o = 176 \text{ mm}$$

