

15
(cont'd)

c) principals from (a)

$\hat{\sigma}, \hat{\tau}$	\sqrt{u} from (10)	v
200, 0	$\max(\frac{200}{250}, 0, \frac{200}{250} - \frac{200}{800}) = 0.8$	1.25
50, -340	$\max(\frac{50}{250}, \frac{340}{800}, \frac{50}{250} + \frac{290}{800}) = 0.56$	1.78
0, -450	$\max(0, \frac{450}{800}, 0 + \frac{450}{800}) = 0.56$	1.78

d) principals from (b) with $v = 0.2$

principals	\sqrt{u} from (10)	v
200, 50, 50	$\max(\frac{200}{250}, \frac{50}{800}, \frac{200}{250} - \frac{250}{800}) = 0.8$	1.25
50, -58, -340	$\max(\frac{50}{250}, \frac{340}{800}, \frac{50}{250} + \frac{290}{800}) = 0.56$	1.78
-130, -200, -450	$\max(\frac{130}{250}, \frac{450}{800}, \frac{130}{250} + \frac{380}{800}) = 0.56$	1.78

16

From (8) with $\sigma_3 = 0$

$$\sigma_E^2 = \frac{1}{2} [(\sigma_1 - \sigma_2)^2 + \sigma_1^2 + \sigma_2^2]$$

$$= \sigma_1^2 - \sigma_1 \sigma_2 + \sigma_2^2$$

If $\sigma_1 = \bar{\sigma} + \bar{\tau}$, $\sigma_2 = \bar{\sigma} - \bar{\tau}$

$$\sigma_E^2 = \bar{\tau}^2 + 3\bar{\sigma}^2$$

If $\bar{\sigma} = (\sigma_x + \sigma_y)/2$

$$\bar{\tau}^2 = \left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2$$

$$\sigma_E^2 = \sigma_x^2 - \sigma_x \sigma_y + \sigma_y^2 + 3\tau_{xy}^2$$

QED.

The first equation

is plotted :-

For pure shear, $\sigma_2 = -\sigma_1$

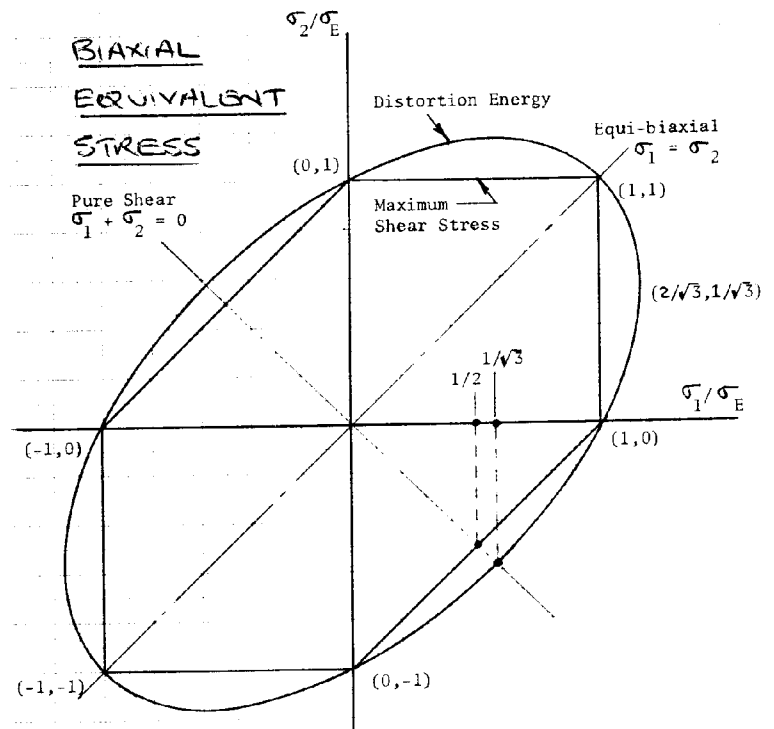
so from first equation

$$\sigma_E^2 = 3\sigma_1^2$$

or, at failure ($v=1$)

$$S = \sqrt{3} S_{\text{shear}}$$

$$\text{i.e. } S_s/S = 1/\sqrt{3} = 0.577$$



For the maximum shear stress theory applied to plane stress ($\sigma_3 = 0$).

From (2) if $\sigma_1 > \sigma_2 > 0$ then $\hat{\sigma} = \sigma_1$; $\hat{\tau} = 0$ & $\sigma_E = \sigma_1$

if $\sigma_1 > 0 > \sigma_2$ then $\hat{\sigma} = \sigma_1$; $\hat{\tau} = \sigma_2$ & $\sigma_E = \sigma_1 - \sigma_2$

which plot as straight lines in first quadrant

(under the equality line) and fourth quadrant.

Considering other inequality sets of $(\sigma_1, \sigma_2, 0)$ leads to complete failure (zero or tension).

Again we note that the max. shear stress theory is more conservative than the distortion energy theory.