

To design a component for safety, all possible failure modes must be examined, and materials/dimensions chosen to prevent failure in any mode.

There are three obvious modes here:

1. Bending of Handle.

Free body of seg. at (i)

The operator's two hands produce the two P's. &

the torque $T = PL$

Assuming $L/D \gg 1/2$ from free body of handle

(ii), max contact force is $PL/D = T/D = 6 \text{ kN}$

And, with same assumption the max bending moment (iii)

is $M = PL = T = 300 \text{ Nm}$.

So, to avoid handle failure in bending :-

$$\hat{\sigma} = M \hat{y} / I \leq 300 \text{ MPa}, \text{ the design stress.}$$

$$\therefore 300 \times 10^3 \times d/2 / \frac{\pi d^4}{32} \leq 300 \quad \text{with } d \text{ in mm}$$

$$\text{N} \cdot \text{mm} \quad \text{mm} \quad \frac{1}{\text{mm}^4} \quad \frac{\text{N}}{\text{mm}^2}$$

i.e. $d \geq 10 \sqrt[3]{(32/\pi)} = 21.7 \text{ mm}$

(This seems excessive, however given the cited material, this minimum must stand).

2. Torque of Tube.

$$\hat{\tau} = Tr / J \leq \hat{\tau}_{\text{all}} \approx 0.5 \times 2.00 \quad \left\{ \begin{array}{l} \text{assuming max.} \\ \text{shear stress} \end{array} \right.$$

to avoid failure.

$$\text{Here: } J = \frac{\pi}{32} [(D+t)^4 - (D-t)^4] = \frac{\pi}{8} D^3 t [1 + (t/D)^2]$$

$$r = \frac{1}{2} (D+t) = \frac{1}{2} D [1 + (t/D)]$$

As a first approx. assume $t/D \ll 1$ then

$$T \leq 2D / \frac{\pi}{8} D^3 t = 2T / \pi D^2 t \leq 100 \text{ MPa}$$

$$\therefore t \geq 2 \times 300 \times 10^3 / \pi \times 50^2 \times 100 = 0.76 \text{ mm.}$$

$$\text{N} \cdot \text{mm} \quad \frac{1}{\text{mm}^2} \quad \frac{\text{mm}}{\text{mm}^2}$$

This minimum, if used, would probably give rise to local buckling - i.e. the tube is far too thin.

However note that we have only considered steady torque, we have not looked at the mechanism whereby torque is transmitted from hole region into body of tube.

3. Contact between Handle & Tube.

From 1. above, max contact force is 6 kN.

Insert into equation developed in preceding problem, with $L \rightarrow t$ and $E^* = \frac{2E}{2 \times 0.91} = 113 \text{ GPa}$